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Implementation of Nonlocal Pansharpening Image Fusion

Joan Duran¹, Antoni Buades², Bartomeu Coll³, Catalina Sbert⁴

¹ Universitat de les Illes Balears, Spain (joan.duran@uib.es)

² Universitat de les Illes Balears, Spain (toni.buades@uib.es)

³ Universitat de les Illes Balears, Spain (tomeu.coll@uib.es)

⁴ Universitat de les Illes Balears, Spain (catalina.sbert@uib.es)

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Abstract

This paper focuses on the implementation of the pansharpened image fusion technique proposed in the companion paper [A Nonlocal Variational Model for Pansharpening Image Fusion, SIAM Journal on Imaging Sciences, 2014, to appear]. Pansharpening refers to the process of inferring a high resolution multispectral image from a high resolution panchromatic image and low resolution multispectral one. Although quite successful in terms of relative error, state-of-the-art pansharpening methods still introduce relevant color artifacts. The variational pansharpening model proposed by Duran et al. incorporates a nonlocal regularization term that takes advantage of image self-similarity, leading to significant reduction of the above-mentioned color artifacts.

Source Code

ANSI C source code to produce the same results as the demo is accessible at the IPOL web page of this article¹.

Keywords: image fusion; pansharpening; multispectral imagery; neighborhood filter; nonlocal operators; energy functional

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1 Introduction

Many Earth observation satellites, such as SPOT, Landsat, IKONOS or QuickBird, provide continuously growing quantities of remote sensing images useful for a wide range of tasks. For example, satellite images are used in feature detection, land cover classification, water depth estimation, soil moisture content, vegetation mapping or many military tasks such as mission planning, navigation and targeting.

Digital color images are usually represented by three color values at each pixel. However, most common cameras use a CCD sensor device measuring a single color per pixel (either red, green or blue). The other two color values of each pixel must be interpolated from the neighboring pixels in the so-called demosaicking process. The selected configuration of the CCD sensor usually follows the CFA Bayer where, out of a group of four pixels, two are green, one is red and one is blue. Most satellites use a different acquisition system that decouples the acquisition of a panchromatic image at high spatial resolution from the acquisition of a multispectral image at lower spatial resolution. The design of multispectral sensors with better resolution is limited by technical constraints of on-board storage and by bandwidth transmission of the images from the satellite to the Earth.

High spatial resolution is necessary to correctly detect shapes, edges and structures. On the contrary, different types of land are better classified using images with multiple spectral bands. Accordingly, the goal of pansharpening image fusion is to integrate the geometric detail of the panchromatic image and the precise spectral information of the multispectral image to produce a high resolution multispectral image. Figure 1 illustrates the pansharpening problem.

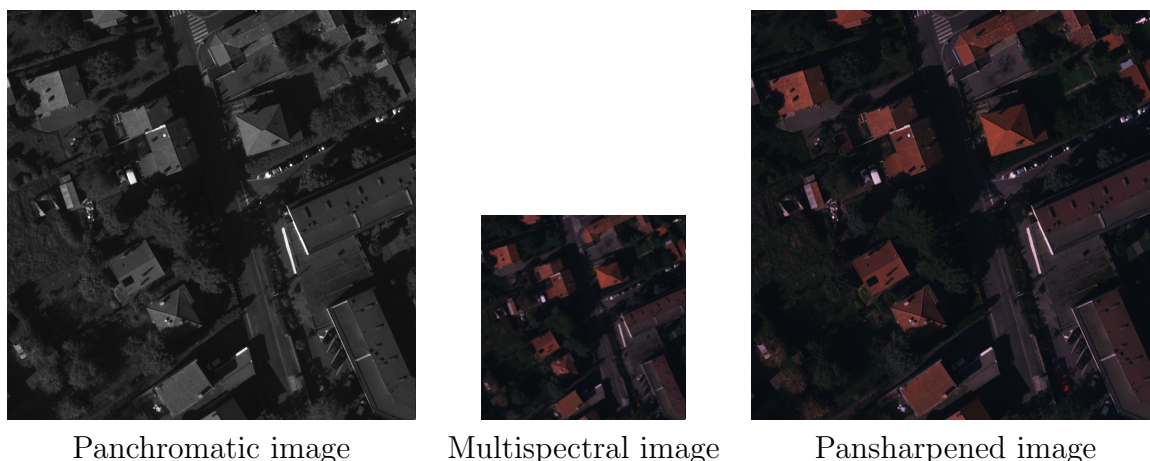


Figure 1: Description of the pansharpening problem. Most satellites provide a high-resolution grayscale image that contains information about shapes, features and structures, and a multispectral image at lower spatial resolution. The goal of pansharpening is to infer a high resolution multispectral image from the previous data.

The pansharpening has been an intensive field of research during the last decades. Initial methods imposed the final color image to match the luminance of the panchromatic image while maintaining the low frequencies of the initial chromatic components. This is the case of the component-substitution techniques, for instance the Intensity-Hue-Saturation (IHS) [12, 5, 17, 21] and the Principal Component Analysis transforms (PCA) [6, 9, 19], or of relative spectral contribution methods, such as intensity modulation [7] and Brovey's method [23]. Several models using discrete wavelet transforms [26, 10, 27, 16, 25] or Laplacian pyramid algorithms [24, 1] have also been proposed. Some recently proposed variational models determine the pansharpened image through the minimization of specific energy functionals [2, 15]. Pansharpening techniques have been extensively reviewed in the literature [22, 20, 8].

Duran et al. [3] proposed a variational pansharpener formulation inspired on the NL-means denoising algorithm [4]. The functional consists of two fidelity terms, which force the pansharpener image to be consistent with panchromatic and multispectral data, and a nonlocal regularization term which acts as a neighborhood filter. The panchromatic image is used to derive nonlocal relationships among patches describing the geometry of the desired pansharpener image. This geometry being available through the panchromatic image, the problem reduces to a linear quadratic system as proposed in [11].

In this paper, we first introduce the nonlocal functional form of the NL-means after which we present the pansharpener model proposed by Duran et al. [3]. Then we focus on the description and implementation of the derived algorithm. Lastly, a detailed performance comparison with some of state-of-the-art methods for pansharpener is presented.

2 Nonlocal Regularization

The NL-means algorithm [4] denoises a pixel $x \in \Omega$ by averaging the values of all pixels whose Gaussian neighborhood looks like the neighborhood of x :

$$\text{NL}[u](x) = \frac{1}{C(x)} \int_{\Omega} e^{-\frac{d_{\rho}(u(x), u(y))}{h^2}} u(y) dy, \quad \forall x \in \Omega,$$

where

$$C(x) = \int_{\Omega} e^{-\frac{d_{\rho}(u(x), u(y))}{h^2}} dy$$

is a normalizing factor and the distance d_{ρ} is given by

$$d_{\rho}(u(x), u(y)) = \int_{\Omega} G_{\rho}(t) |u(x+t) - u(y+t)|^2 dt.$$

In this framework, G_{ρ} is a Gaussian kernel and h acts as a filtering parameter. The parameter h controls the decay of the exponential function and, therefore, the decay of the weights as a function of the Euclidean distances.

Kindermann et al. [13] were the first to formulate the NL-means algorithm as a variational method. They interpreted the NL-means, and the neighborhood filters in general, as regularizations based on nonlocal functionals in the general form

$$\int_{\Omega} \int_{\Omega} g \left(\frac{|u(x) - u(y)|^2}{h^2} \right) w(|x - y|) dx dy,$$

where $w(|x - y|)$ is a spatial weight function. Similar approaches have been introduced for many image processing applications where classical TV minimization [18] is replaced by nonlocal regularization terms. Gilboa and Osher [11] considered the general quadratic nonlocal functional

$$J(u) = \int_{\Omega} \int_{\Omega} (u(x) - u(y))^2 w_{u_0}(x, y) dx dy, \quad (1)$$

where $w_{u_0}(x, y)$ now depends on the initial image u_0 . The weight function w_{u_0} is always assumed nonnegative and symmetric. Gilboa and Osher [11] minimized $J(u)$ with a gradient descent method derived from the associated Euler-Lagrange equation, that is,

$$u_{n+1}(x) = \frac{1}{C(x)} \int_{\Omega} u_n(y) w_{u_0}(x, y) dy,$$

where $C(x) = \int_{\Omega} w_{u_0}(x, y) dy$ is a normalizing factor and u_0 is given as an initial condition of the process. This formulation is a linear and powerful tool for image processing since the weight distribution is independent of u and there is no restriction on the way the initial condition is computed.

3 The Pansharpening Model

The pansharpening model proposed by Duran et al. [3] is based on a variational formulation and it is related to the works of Ballester et al. [2] and of Gilboa and Osher [11].

Let us denote by $\vec{u} = (u_1, \dots, u_M)$ the true multispectral image defined on an open bounded domain $\Omega \subset \mathbb{R}^N$, where M is the number of spectral channels. Each coordinate $u_m : \Omega \rightarrow \mathbb{R}$, $1 \leq m \leq M$, represents the intensity corresponding to the m -th spectral band. For color images, $M = 3$ and the usual red, green and blue channels are considered. The available data is composed by the panchromatic image P defined in the same domain Ω and the observed spectral components, $\vec{u}^S = (u_1^S, \dots, u_M^S)$, defined on a sampled grid $S \subseteq \Omega$, $u_m^S : S \rightarrow \mathbb{R}$, whose points will be called the low-resolution pixels.

We propose to minimize a functional consisting of a nonlocal regularization term and two fidelity terms, which force the pansharpened image to be consistent with panchromatic and low-resolution multispectral data.

Regularization term. The panchromatic image is used to derive nonlocal relationships among patches. Accordingly, we introduce a quadratic regularization term as in (1) with the weight distribution given by

$$\omega(x, y) = \frac{1}{C(x)} e^{-\frac{d_\rho(P(x), P(y))}{h^2}}, \quad (2)$$

where

$$C(x) = \int_{\Omega} e^{-\frac{d_\rho(P(x), P(y))}{h^2}} dy. \quad (3)$$

Note that $\omega(x, y)$ satisfies the usual conditions $0 \leq \omega(x, y) \leq 1$ and $\int_{\Omega} \omega(x, y) dy = 1$, but the normalization using (3) breaks down the symmetry of the weights between two given pixels in the image. By using (2)-(3), the geometry of the panchromatic is transported to the pansharpened image.

Panchromatic constraint. We assume that the panchromatic image and the spectral bands are geometrically aligned. Thus P should be a linear combination of the different channels of the multispectral image, that is,

$$P(x) = \sum_{m=1}^M \alpha_m u_m(x), \quad \forall x \in \Omega,$$

where $\alpha_m \geq 0$, $1 \leq m \leq M$, and $\sum_m \alpha_m = 1$.

Spectral constraint. The low-resolution image is assumed to be related to the high-resolution one by a low-pass filtering followed by subsampling, which writes as

$$k_m * u_m(p) = u_m^S(p), \quad \forall p \in S, \quad \forall 1 \leq m \leq M,$$

where k_m is the impulse response for the spectral channel u_m . In order to preserve the frequency information from the original low-resolution multispectral image \vec{u}^S , the following term is considered in the energy functional

$$\int_{\Omega} \Pi_S \cdot (k_m * u_m(x) - u_m^\Omega(x))^2 dx, \quad \forall 1 \leq m \leq M, \quad (4)$$

where $\Pi_S = \sum_{p \in S} \delta_p$ is a Dirac's comb defined by the sampling grid S , and each u_m^Ω denotes an arbitrary extension of u_m^S as a continuous function from S to Ω . This integral of a sum of Dirac's is unambiguous as we assume that no point of S belongs to the boundary of Ω . Furthermore, since the integrand term is multiplied by Π_S , the integral expression (4) does not depend on the particular extension u_m^Ω .

By taking into account the regularization term and the constraints imposed by the data generation model, Duran et al. [3] propose to minimize the following energy functional

$$\begin{aligned}
 J(\vec{u}) &= \frac{1}{2} \sum_{m=1}^M \int_{\Omega} \int_{\Omega} (u_m(x) - u_m(y))^2 \omega(x, y) dx dy \\
 &+ \frac{\lambda}{2} \int_{\Omega} \left(\sum_{m=1}^M \alpha_m u_m(x) - P(x) \right)^2 dx \\
 &+ \frac{\mu}{2} \sum_{m=1}^M \int_{\Omega} \Pi_S \cdot (k_m * u_m(x) - u_m^{\Omega}(x))^2 dx,
 \end{aligned} \tag{5}$$

where $\lambda, \mu > 0$ are weighting parameters. The same authors [3] show that there exists a unique minimizer for (5) in a specific class of functions linked to a weighted L^2 space. The associated Euler-Lagrange equation to be solved for each channel u_m , $1 \leq m \leq M$, is given by

$$-Lu_m(x) + \lambda \alpha_m \left(\sum_{k=1}^M \alpha_k u_k(x) - P(x) \right) + \mu (k_m^{\top} * (\Pi_S \cdot (k_m * u_m - u_m^{\Omega}))) (x) = 0, \quad \forall x \in \Omega, \tag{6}$$

where k_m^{\top} is the kernel adjoint defined as $k_m^{\top}(x) = k_m(-x)$ and the integral operator L is given by

$$Lu_m(x) = \int_{\Omega} (u_m(y) - u_m(x)) (\omega(x, y) + \omega(y, x)) dy, \quad \forall 1 \leq m \leq M.$$

4 Discrete Algorithm

Let the panchromatic image P be defined on a discrete grid $I = \{0, 1, \dots, N-1\} \times \{0, 1, \dots, N-1\}$ and $p = (p_i, p_j) \in I$ denote an image pixel. Let the spectral components u_1^S, \dots, u_M^S be defined on a lower resolution grid S of size $\frac{N}{s} \times \frac{N}{s}$, where s is the sampling factor.

Applying the gradient descent method to minimize (5) computes the solution of (6) iterating the equation

$$\begin{aligned}
 u_m^{(n+1)}(p) &= u_m^{(n)}(p) - \Delta t \sum_{q \in I} (u_m^{(n)}(p) - u_m^{(n)}(q)) (\omega(p, q) + \omega(q, p)) \\
 &- \Delta t \lambda \alpha_m \left(\sum_{k=1}^M \alpha_k u_m^{(n)}(p) - P(p) \right) - \Delta t \mu (k_m^{\top} * (\Pi_S \cdot (k_m * u_m^{(n)} - u_m^{\Omega}))) (p), \quad \forall p \in I,
 \end{aligned} \tag{7}$$

for each band u_m , $1 \leq m \leq M$. In this setting, $n \geq 0$ is the iteration number, $\Delta t > 0$ stands for the artificial time step in the descent direction and u_m^{Ω} is an arbitrary extension of the low-resolution band u_m^S to the whole grid I by means of, for instance, a simple replication by s factor. Recall that Π_S indicates which of the pixels in the high resolution image we actually know from the low resolution image. Accordingly, the discrete version of Π_S is considered here as a $N \times N$ matrix such that $\Pi_S(p_i, p_j) = 1$ if $(p_i, p_j) \in S$ and $\Pi_S(p_i, p_j) = 0$ otherwise. Note that this formulation requires an initialization of each u_m .

For computational purposes, the regularity term is restricted to pixels at a certain distance from the current pixel (support zone). That is, the weight distribution $\omega(p, q)$ will be zero for pixels such that $\|p - q\|_{\infty} > K$, for a certain positive parameter K . Therefore, the similarity between pixels p and q is measured as

$$\omega(p, q) = \begin{cases} \frac{1}{C(p)} e^{-\frac{1}{K^2} \sum_{t \in \mathcal{N}_0} \|P(p+t) - P(q+t)\|^2} & \text{if } \|p - q\|_{\infty} \leq K, \\ 0 & \text{otherwise,} \end{cases}$$

with the normalizing factor $C(p)$ defined by

$$C(p) = \sum_{\{q: \|q-p\|_\infty \leq K\}} e^{-\frac{1}{h^2} \sum_{t \in \mathcal{N}_0} \|P(p+t) - P(q+t)\|^2},$$

where \mathcal{N}_0 is an $l \times l$ discrete window centered at $(0, 0)$ (comparison window). Note that the Gaussian kernel G_ρ introduced in the mathematical formulation is not considered here as it is only necessary when the size of the window increases considerably. Furthermore, the weight of the reference pixel, $\omega(p, p)$, is set to the maximum of the weights $\omega(p, q)$ for $q \neq p$. This setting avoids the excessive weighting of the reference point. Due to the fast decay of the exponential kernel, large Euclidean distances yield nearly zero weights, acting as an automatic threshold. The decay of the exponential functions, and thus the decay of the weights, is controlled by the parameter h .

In (7) note that, since the weights are computed on the panchromatic image, they are not modified during the evolution procedure, so they are computed only once. The complexity associated to the precomputation of the weights puts this algorithm at a computational cost higher than basic pansharpening methods. Multiresolution and preselection strategies can be used to further accelerate the patch comparisons [4, 14].

The whole algorithm is described by the pseudo-code in algorithm 1, which takes as input images the high-resolution panchromatic, the extension of the multispectral data to the whole grid and an arbitrary initialization. The first step of the proposed algorithm consists in computing the weight distribution on the panchromatic image. After that, the solution of the pansharpening problem is obtained by iterating equation (7) for a certain number of iterations.

5 Experimental Results

In this section we present experimental results illustrating the behavior of algorithm 1 for pansharpening image fusion. Experiments were performed on natural images and on full color aerial images furnished to us by CNES, Centre National d'Études Spatiales. In both cases we simulated panchromatic and subsampled spectral components from the ‘‘ground truth’’ reference images in the following terms. The panchromatic image was obtained by the average of the available channels, that is, the mixing coefficients were set to $\alpha_m = \frac{1}{M}$, $1 \leq m \leq M$. The low-resolution multispectral image was simulated by Gaussian convolution followed by subsampling. We used a sampling factor $s = 4$ with a corresponding Gaussian convolution of standard deviation $\sigma = 2.2$.

First, we present a detailed comparison of the proposed algorithm with some relevant state-of-the-art techniques applied to natural images. We shall compare with IHS [12], Brovey [23], Wavelets-based [26] and P+XS [2]. The initialization used for the IHS method is a simple interpolation by splines, whereas all other algorithms are initialized with the pansharpened image provided by IHS. The parameters of our algorithm were selected as follows: $\lambda = 100$, $\mu = 100 \cdot s^2$ (the parameter is normalized depending on the sampling factor s), $K = 3$ (the size of the support zones is 7×7 pixels), $l = 3$ (the size of the comparison window is 3×3 pixels) and $\Delta t = 0.01$. The filtering parameter controlling the decay of the weights was selected depending on the sampling factor, namely $h = 6$ if $s = 4$ and $h = 1.25$ if $s = 2$. As stopping criterion, we used a tolerance value of $\varepsilon = 10^{-3}$ for the relative error between two consecutive iterations. Anyway, we stopped the algorithm after $N_{iter} = 100$ iterations even if the tolerance was not reached. The extended image \bar{u}^Ω required in the scheme (7) was constructed by means of a simple replication by a factor s .

Figures 2 and 3 illustrate how the colors from the original low resolution multispectral images are not necessarily preserved. The pansharpened image provided by the wavelet-based technique presents several color artifacts which mainly appear at edges. IHS and Brovey give results with high spatial resolution, however, a loss of spectral information occurs. For instance, the color of the balloon basket

Algorithm 1 Nonlocal pansharpening algorithm**Input:**

- $P \leftarrow$ panchromatic image given on the high-resolution grid I
- $\vec{u}^\Omega = (u_1^\Omega, \dots, u_M^\Omega) \leftarrow$ arbitrary extension of the multispectral data to the whole grid
- $\vec{u}^0 \leftarrow$ arbitrary initialization
- $\alpha_1, \dots, \alpha_M \in [0, 1] \leftarrow$ mixing coefficients
- $k_1, \dots, k_M \leftarrow$ impulse responses as two-dimensional matrices
- $\Pi_S \leftarrow$ Dirac's comb as a $N \times N$ binary matrix
- $\lambda, \mu \geq 0 \leftarrow$ trade-off parameters
- $h > 0 \leftarrow$ filtering parameter for the weight distribution
- $K \in \mathbb{Z}^+ \leftarrow$ spatial support for searching similarities (support zone)
- $l \in \mathbb{Z}^+ \leftarrow$ size of \mathcal{N}_0 for computing distances on P (comparison window)
- $\Delta t > 0 \leftarrow$ time-step parameter
- $N_{iter} \in \mathbb{Z}^+ \leftarrow$ number of iterations of the algorithm

Output: pansharpened image $\vec{u} = (u_1, \dots, u_M)$

```

for all pixel  $p \in I$  do                                 $\triangleright$  Pre-computation of the weights on the panchromatic image
   $C(p) \leftarrow 0$ 
  for all pixel  $q \in I, q \neq p$  do
    if  $\|p - q\| \leq K$  then
       $\omega(p, q) \leftarrow e^{-\frac{1}{h^2} \sum_{t \in \mathcal{N}_0} \|P(p+t) - P(q+t)\|^2}$ 
       $C(p) \leftarrow C(p) + \omega(p, q)$ 
    else
       $\omega(p, q) \leftarrow 0$ 
    end if
  end for
   $\omega(p, p) \leftarrow \max\{\omega(p, q) : q \in I, q \neq p\}$ 
  for all pixel  $q \in I$  such that  $\|p - q\| \leq K$  do
     $\omega(p, q) \leftarrow \frac{\omega(p, q)}{C(p)}$ 
  end for
end for
 $\vec{u} \leftarrow \vec{u}^0$ 
 $n \leftarrow 1$ 
while  $n \leq N_{iter}$  do                                 $\triangleright$  Iteration of the explicit scheme (7)
  for all spectral channel  $1 \leq m \leq M$  do
    for all pixel  $p \in I$  do
       $u_m(p) \leftarrow u_m(p) - \Delta t \sum_{q \in I} (u_m(p) - u_m(q)) (\omega(p, q) + \omega(q, p))$ 
       $- \Delta t \lambda \alpha_m \left( \sum_{k=1}^M \alpha_k u_m(p) - P(p) \right)$ 
       $- \Delta t \mu \left( k_m^\top * (\Pi_S \cdot (k_m * u_m - u_m^\Omega)) \right) (p)$ 
    end for
  end for
   $n \leftarrow n + 1$ 
end while
return  $\vec{u} = (u_1, \dots, u_M)$ .

```

in figure 2 has clearly changed from brownish to grayish. A similar spectral distortion is also apparent in the result provided by P+XS. On the other hand, the proposed algorithm meaningfully reduces color artifacts outperforming all the compared techniques. This visual comparison is supported by the Root-Mean-Squared Error (RMSE) computed in RGB coordinates between the reference image and each of the results obtained after applying the above-mentioned pansharpening techniques. If we denote by $\vec{u}^R = (u_1^R, u_2^R, u_3^R)$ the reference image, then the formula for RMSE is given by

$$\text{RMSE} = \frac{1}{3} \sum_{m=1}^3 \sqrt{\frac{\sum_{p \in I} (u_m(p) - u_m^R(p))^2}{N^2}}.$$

Brovey, P+XS and IHS have a similar performance in terms of RMSE, their error being larger than the proposed one.

Figure 4 illustrates the preservation of the spatial information contained in the panchromatic image. For that purpose, the grayscale versions of the fused images were computed. All results displayed in figure 4 compare favorably to the original panchromatic image, so that edges, textures and other geometric details are highly preserved. We want to emphasize that algorithm 1 also performs a slight denoising since it reduces the inherent noise that appears, for instance, at the bow hull of the boat.

We test now all pansharpening techniques under comparison on a multispectral aerial image using three bands (red, green and blue). The goal is to check if the self-similarity underlying the model proposed by Duran et al. [3] holds for aerial images as natural images do. Figure 5 illustrates a comparative visual quality assessment of fused images. For a better visual analysis, we display the difference images between the reference one and the pansharpened results. Once again, IHS, Brovey, Wavelet-based and P+XS techniques suffer from spectral distortion. Indeed, color saturation is significantly reduced on the results provided by these methods, see for instance the red cars or the thin wall appearing in the images. The algorithm discussed in this paper outperforms all other techniques since the difference image displayed in figure 5 contains less amount of information. Note that the proposed algorithm is also the best one in terms of root-mean-squared error.

Finally, we tested algorithm 1 on an aerial hyperspectral image furnished by the CNES. The low-resolution hyperspectral image has four channels (red, green, blue and near-infrared) with a resolution corresponding to one quarter of the panchromatic one. Furthermore, the algorithm was now initialized by a simple replication of each spectral component. Figure 6 shows the reference, the low-resolution and the pansharpened color images involving red, green and blue channels. It also displays false color images using the near-infrared, red and green spectral bands (in this order) in place of the usual RGB. At a glance, the results give good spatial resolution since the images look clear. Furthermore, the spectral information is highly preserved and no artifacts are perceptible.

6 On Line Demo

An online demo of the nonlocal variational model is available at the [web page of this article](#)². The purpose is to simulate the pansharpening problem and to solve it by means of the proposed algorithm. The ANSI C source code (documented) used in this on line demo is also available at the web page.

The program inputs are the RGB image and the sampling factor ($s = 2$ or $s = 4$). The other parameters are fixed as indicated previously, but the users can download the source code and try by themselves. Furthermore, one can upload its own input image or use any of the images available on the demo page. The proposed images have almost no noise. They were obtained by taking good quality photographs in full daylight and then zooming them out by an 8-factor.

²<https://doi.org/10.5201/ipol.2014.98>

The implementation simulates the panchromatic and low-resolution multispectral images from the input. The initialization is then computed by IHS transform and the extended image is given by a simple replication of the low-resolution image by a factor s . The algorithm finally computes the high resolution multispectral image.

The outputs are the reference RGB image, the panchromatic image, the low-resolution image, the initialization provided by IHS, the pansharpened image, the residual images corresponding to the initialization and the solution (difference between the corresponding image and the reference one with stretched dynamic on $[0, 255]$ by an affine contrast change), and the RMSE of both the initialization and the pansharpened images.

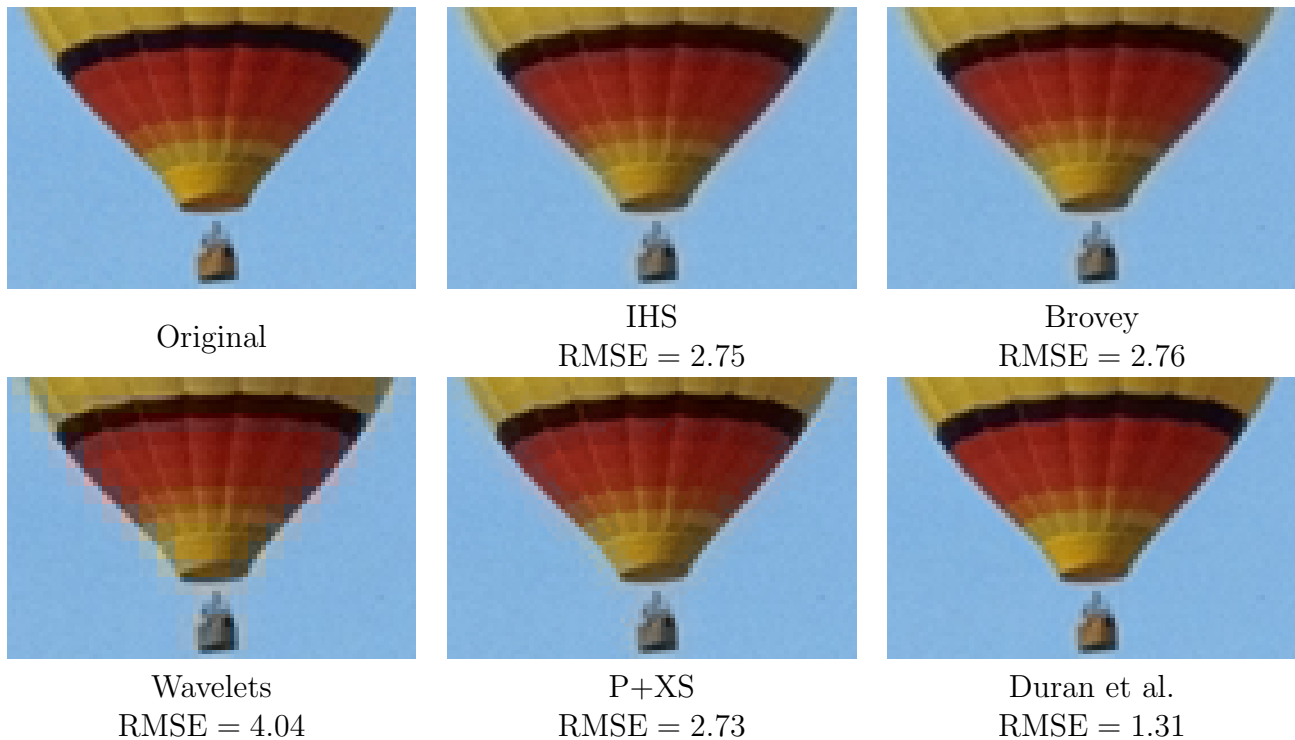


Figure 2: Original color image and the pansharpened images provided by each technique, with sampling factor $s = 4$. We also exhibit the RMSE values between the reference image and each pansharpened result. All techniques perform similarly in terms of spatial quality or geometry except for the wavelet-based one which presents artifacts at the edges of the balloon. In terms of spectral quality, the model proposed by Duran et al. [3] outperforms all other methods. Indeed, the color of the balloon basket has changed from brownish to grayish in the results provided by IHS, Brovey, Wavelet-based and P+XS techniques. Similar effects can also be observed on the balloon stripes where red and yellow are mixed resulting on a browner stripe. All these color artifacts are reduced with the proposed algorithm which is able to better preserve the original colors.

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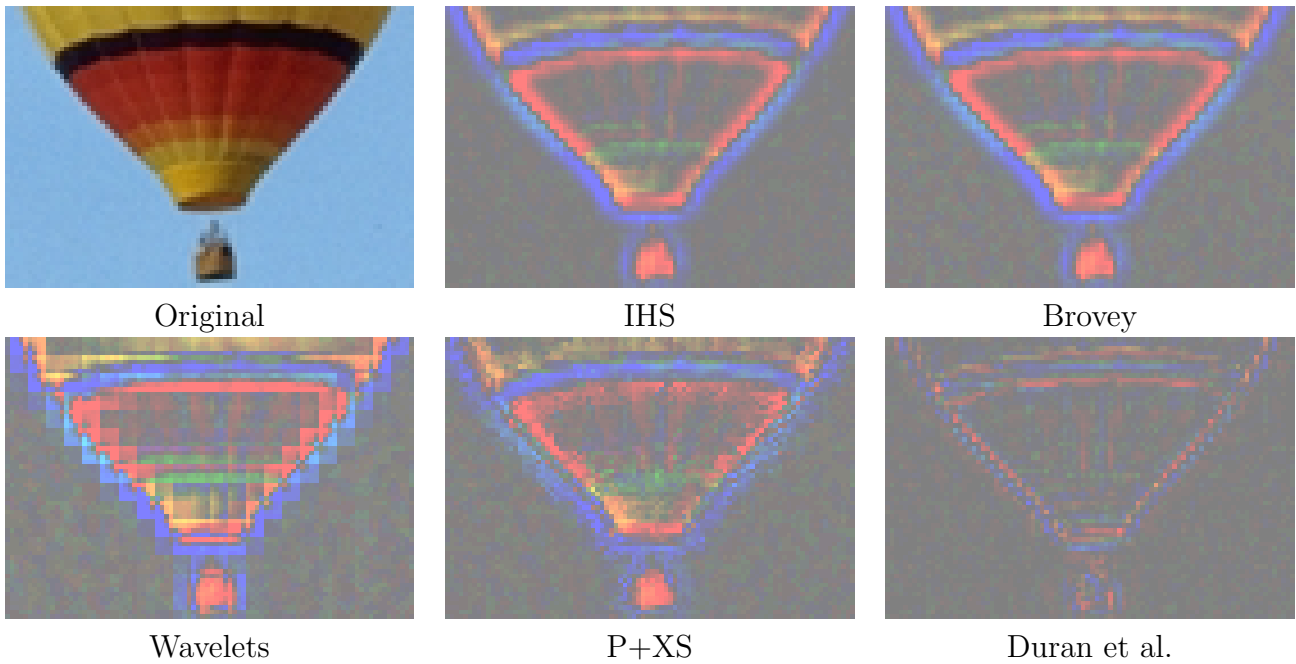


Figure 3: Difference images between the original and the pansharpened images from figure 2. Pixel values have been rearranged from $[-25, 25]$ to $[0, 250]$ for better visibility. We observe that IHS, Brovey, Wavelet-based and P+XS techniques lead to the loss of spectral information. Although a slight color distortion remains, the proposed algorithm is able to better preserve the chromacity of the original image.

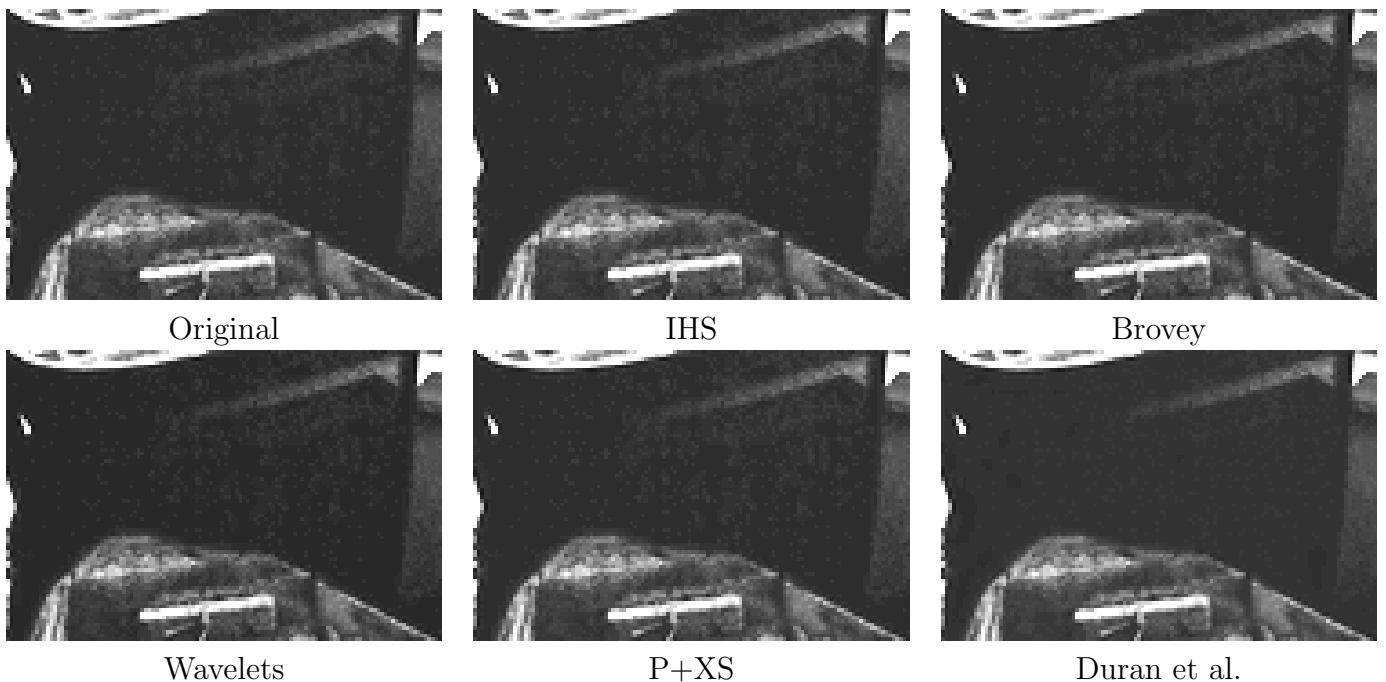


Figure 4: Original panchromatic image and the grayscale versions of the pansharpened images provided by each technique, with sampling factor $s = 4$. Pixel values have been rearranged to $[0, 50]$ for better visibility. All results compare favorably to the original panchromatic, so that edges, textures and other geometric details are highly preserved. Note that the proposed algorithm also performs denoising since it reduces the inherent noise that appears, for instance, at the bow hull of the boat.

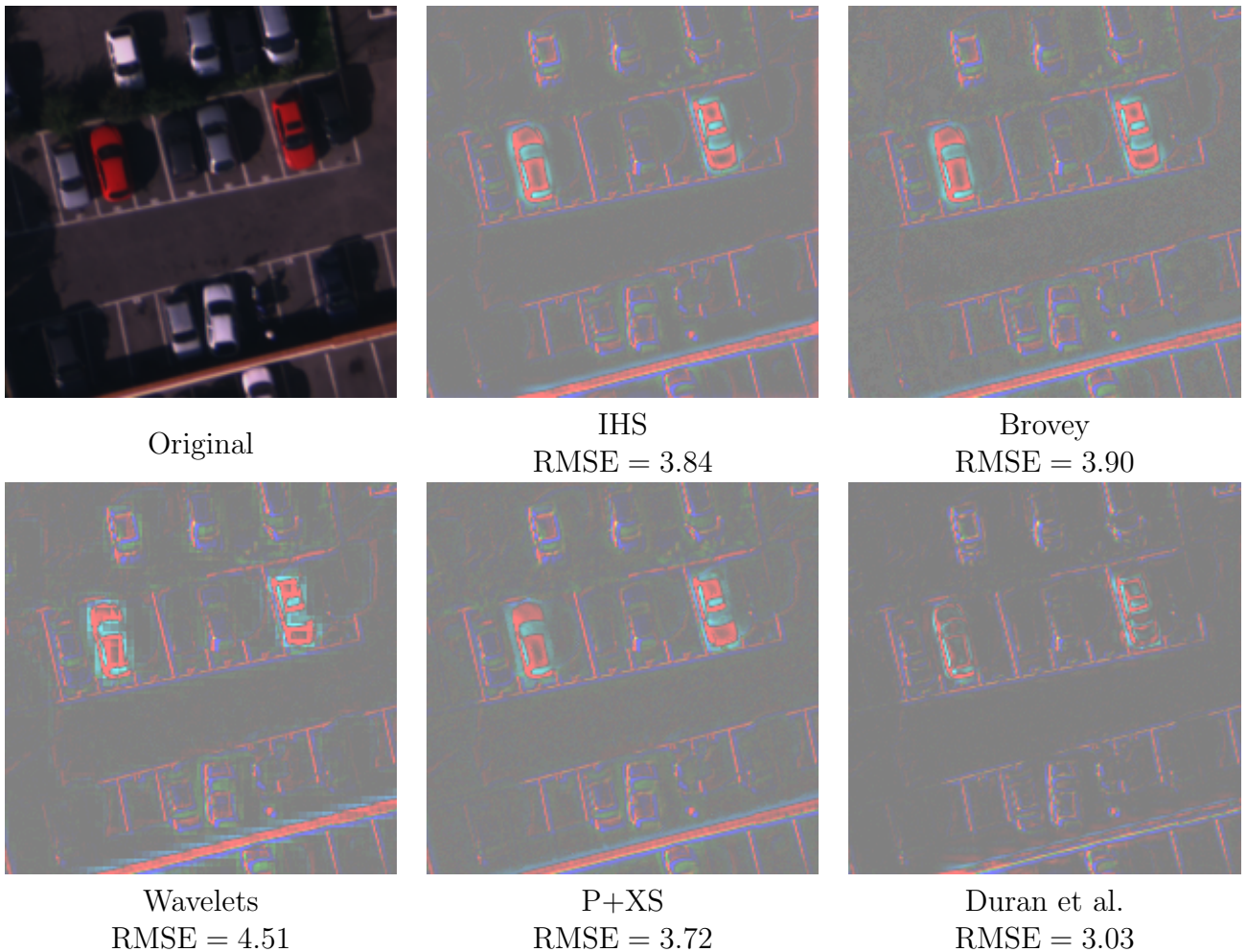


Figure 5: Experiment with an RGB aerial image using $s = 4$ as sampling factor. We exhibit the difference images between the reference one and the pan-sharpened results provided by each method under comparison. Pixel values have been rearranged from $[-25, 25]$ to $[0, 255]$ for better visibility. Furthermore, the RMSE values between the original image and the pan-sharpened ones are displayed. To a greater or lesser extent, we observe that IHS, Brovey, Wavelet-based and P+XS techniques lead to the loss of spectral information. For instance, the color saturation of reddish objects as cars have been significantly reduced on the results provided by these methods. On the contrary, the model proposed by Duran et al. [3] is able to better preserve the chromacity and, thus, the difference image contains less amount of information.

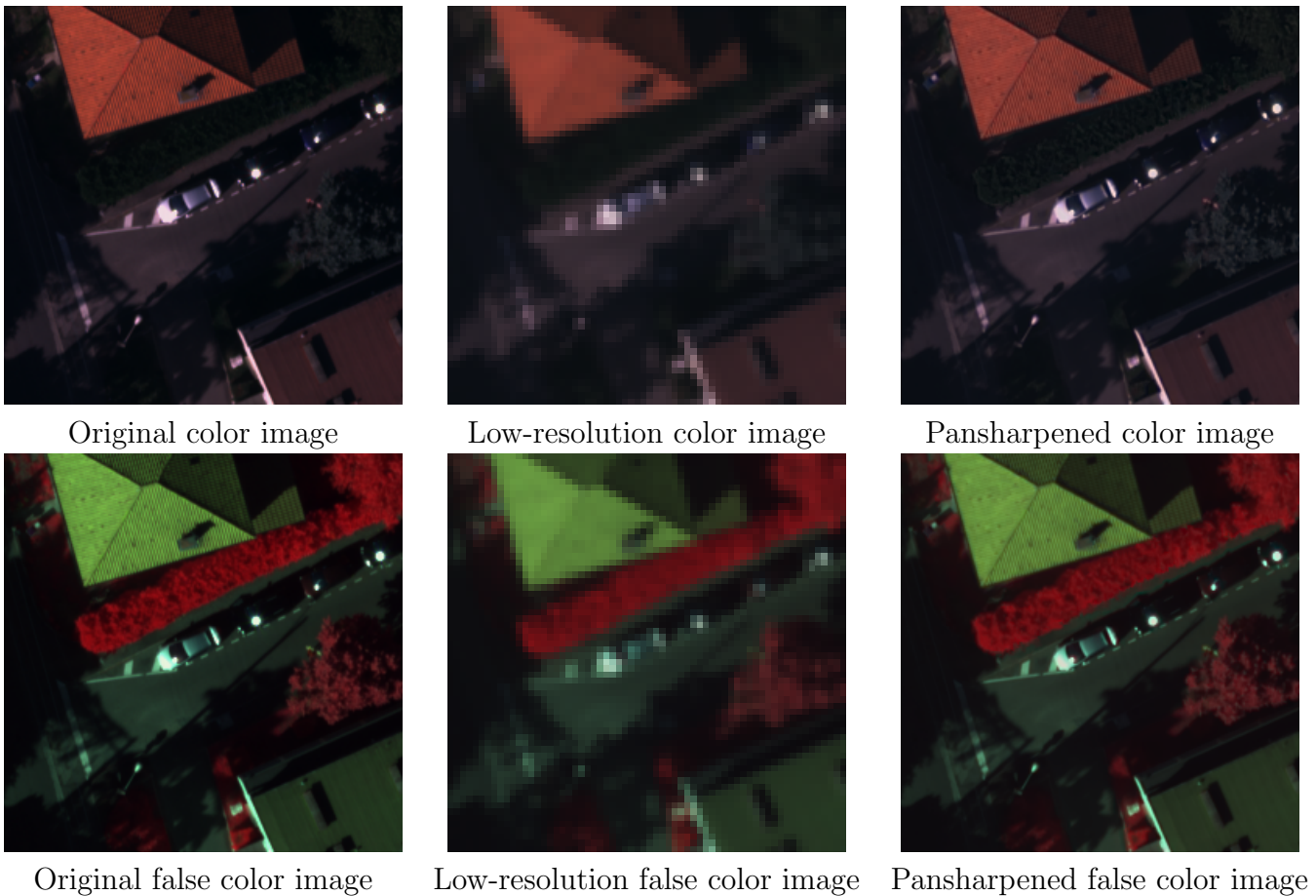
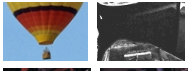


Figure 6: Test of algorithm 1 on a four band aerial image using $s = 4$ as sampling factor. The first row displays the original, the low-resolution and the pansharpened color images involving red, green and blue channels. On the other hand, the second row exhibits the original, the low-resolution and the pansharpened false color images involving near-infrared, red and green spectral bands (in this order) in place of the usual RGB. The size of low-resolution images is 64×64 pixels, whereas the size of original and pansharpened images is 256×256 pixels.

Image Credits



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